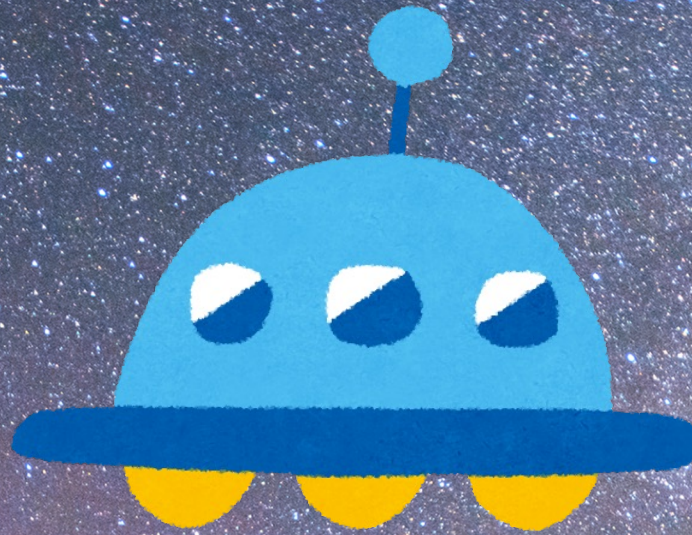


data61/PSL



Abduction Prover in Isabelle(/HOL)

Yutaka Nagashima (the Czech Academy of Sciences)

Daniel Sebastian Goc

x/twitter: YutakangE

✓ high-level talk

✓ installation



LIVE DEMO
(We're almost at the end of this talk.)



3 take-home lessons:

- ① abduction using modus ponens
- ② tactics = conjecturing
- ③ tree search -> graph expansion

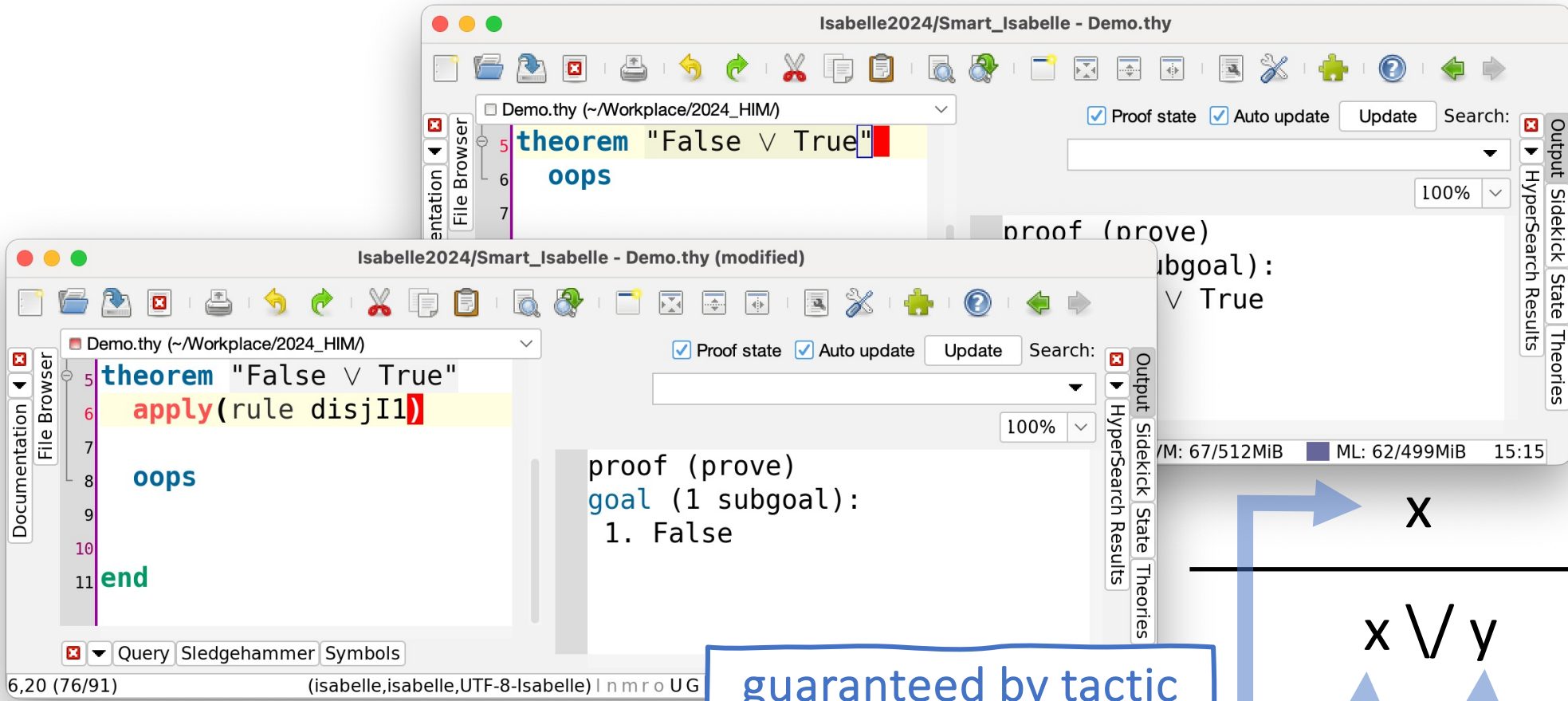
UR ■ United Reasoning

Visit:

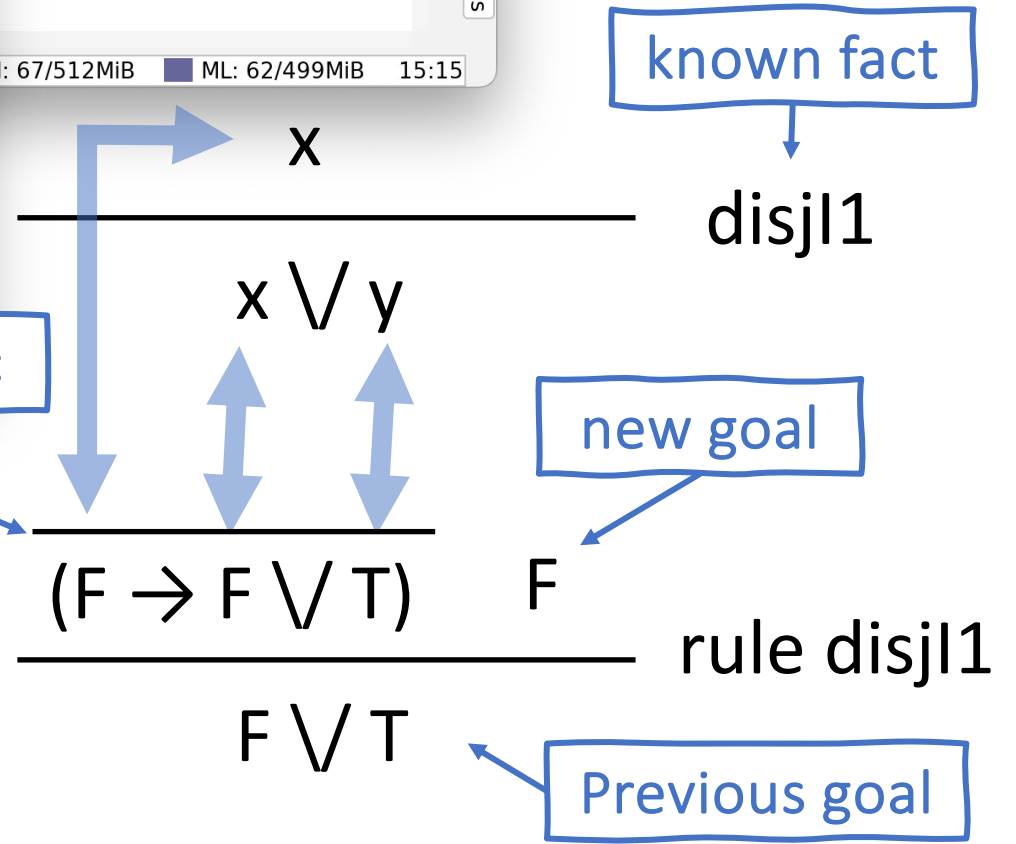
https://youtu.be/rXU-IJxP_GI

LIVE DEMO

(We will come back at the end.)



guaranteed by tactic



Isabelle2024/Smart_Isabelle - Demo.thy

```

5 theorem "False ∨ True"
6   oops
7
proof (prove)
  subgoal)
  ∨ True
end

```

Isabelle2024/Smart_Isabelle - Demo.thy (modified)

```

5 theorem "False ∨ True"
6   apply(rule disjI1)
7
8   oops
9
10
11 end

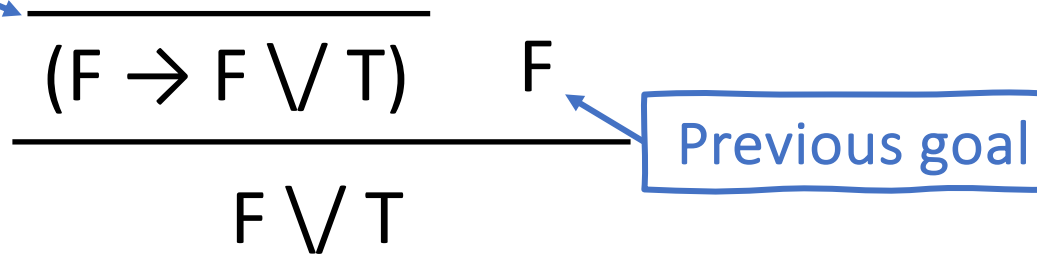
```

proof (prove)
goal (1 subgoal):
1. False

guaranteed by tactic

Previous goal

6,20 (76/91) (isabelle,isabelle,UTF-8-Isabelle) | n m r o U G



```

Isabelle2024/Smart_Isabelle - Demo.thy
5 theorem "False ∨ True"
6   oops
7
8
9
10
11 end
  
```

```

Isabelle2024/Smart_Isabelle - Demo.thy (modified)
5 theorem "False ∨ True"
6   apply(rule disjI2)
7   oops
8
9
10
11 end
  
```

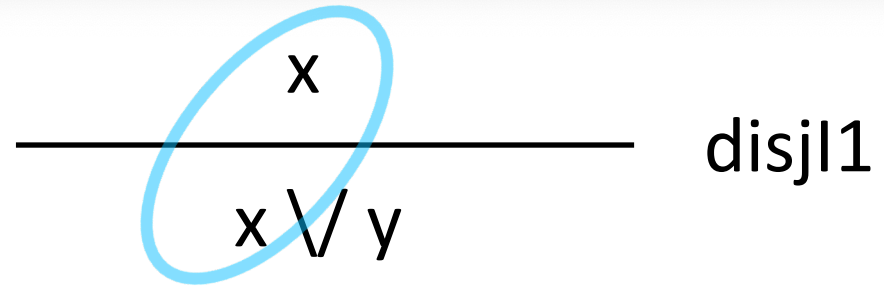
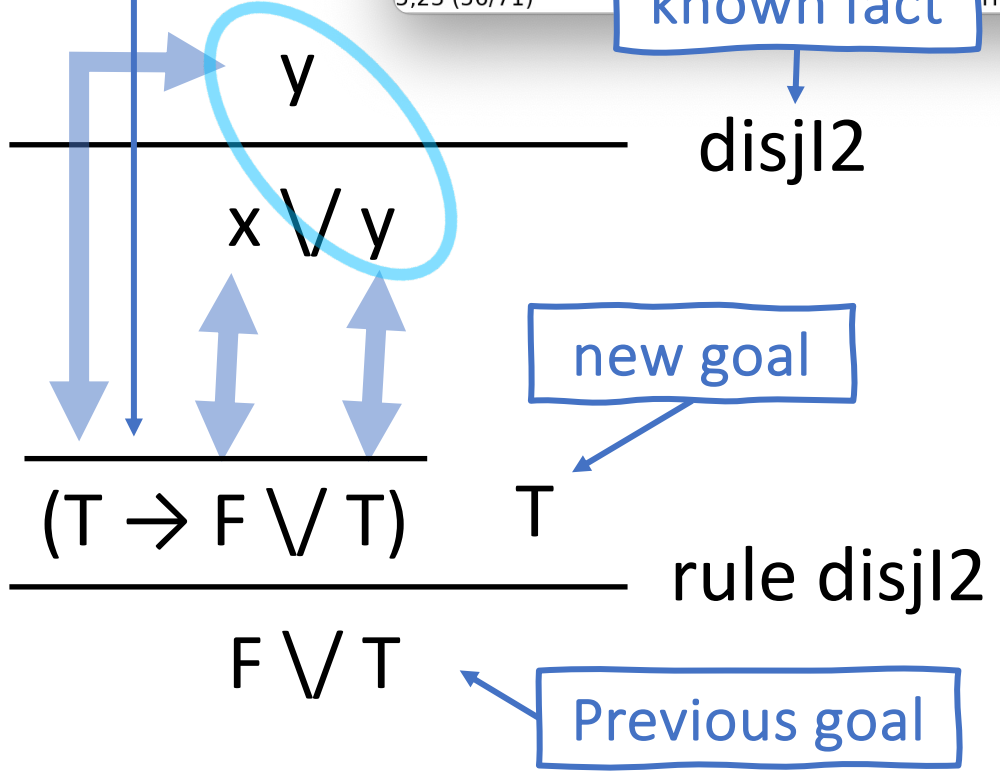
proof (prove)
goal (1 subgoal):
1. True

guaranteed by tactic

known fact

new goal

Previous goal



```

Isabelle2024/Smart_Isabelle - Demo.thy
5 theorem "False ∨ True"
6  oops
7
8 TrueI
9
10
11 end
  
```

known fact

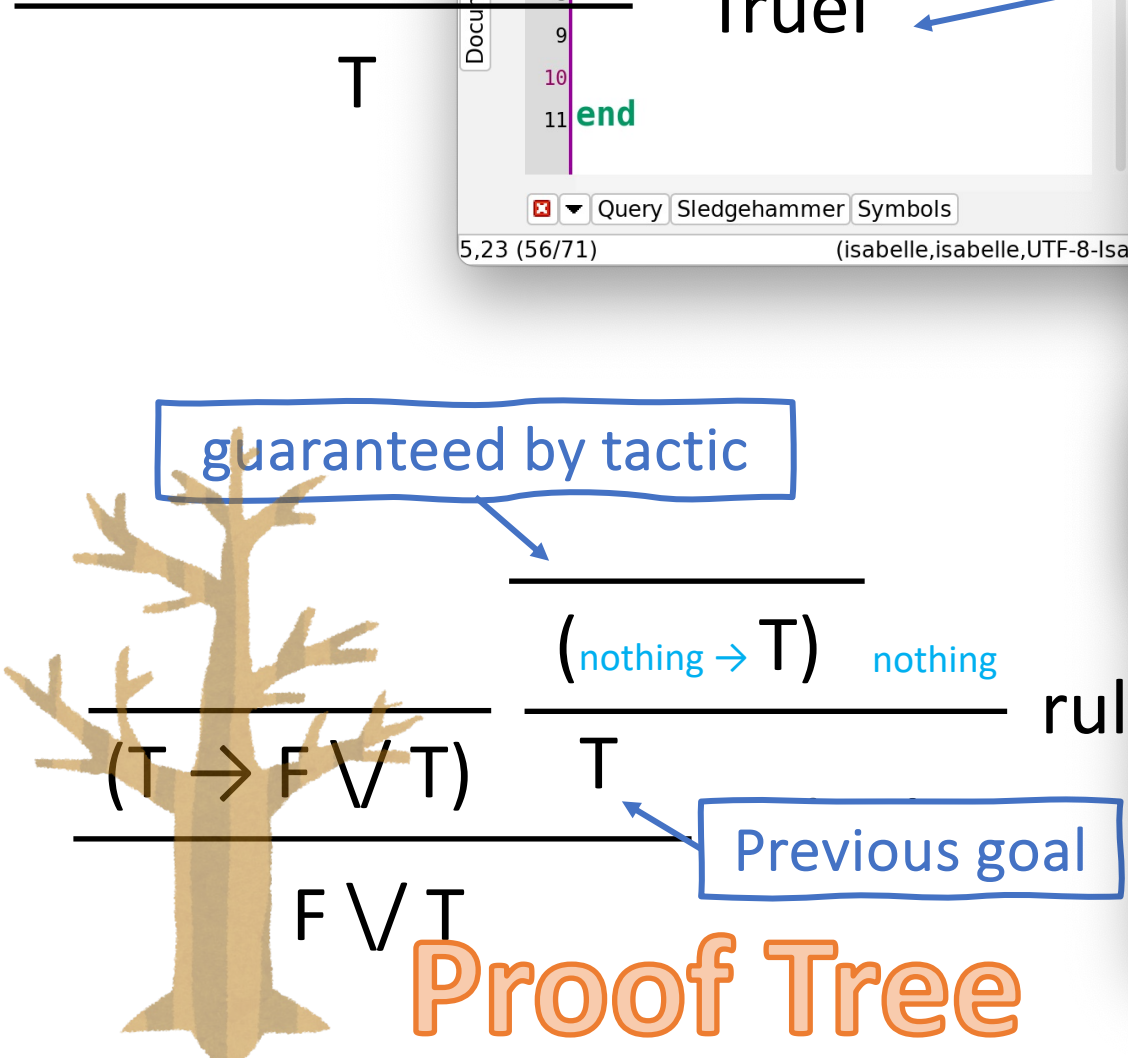
```

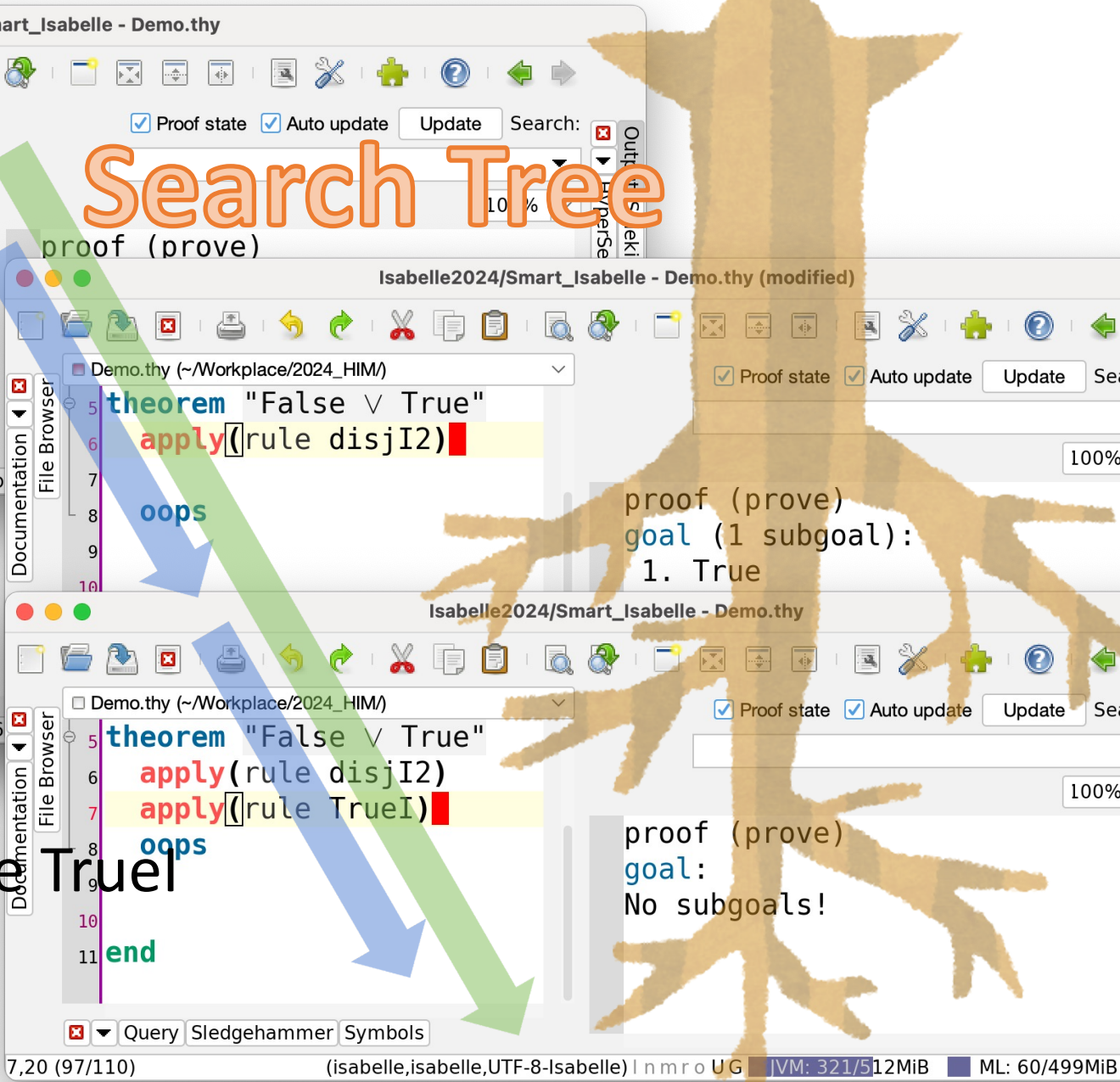
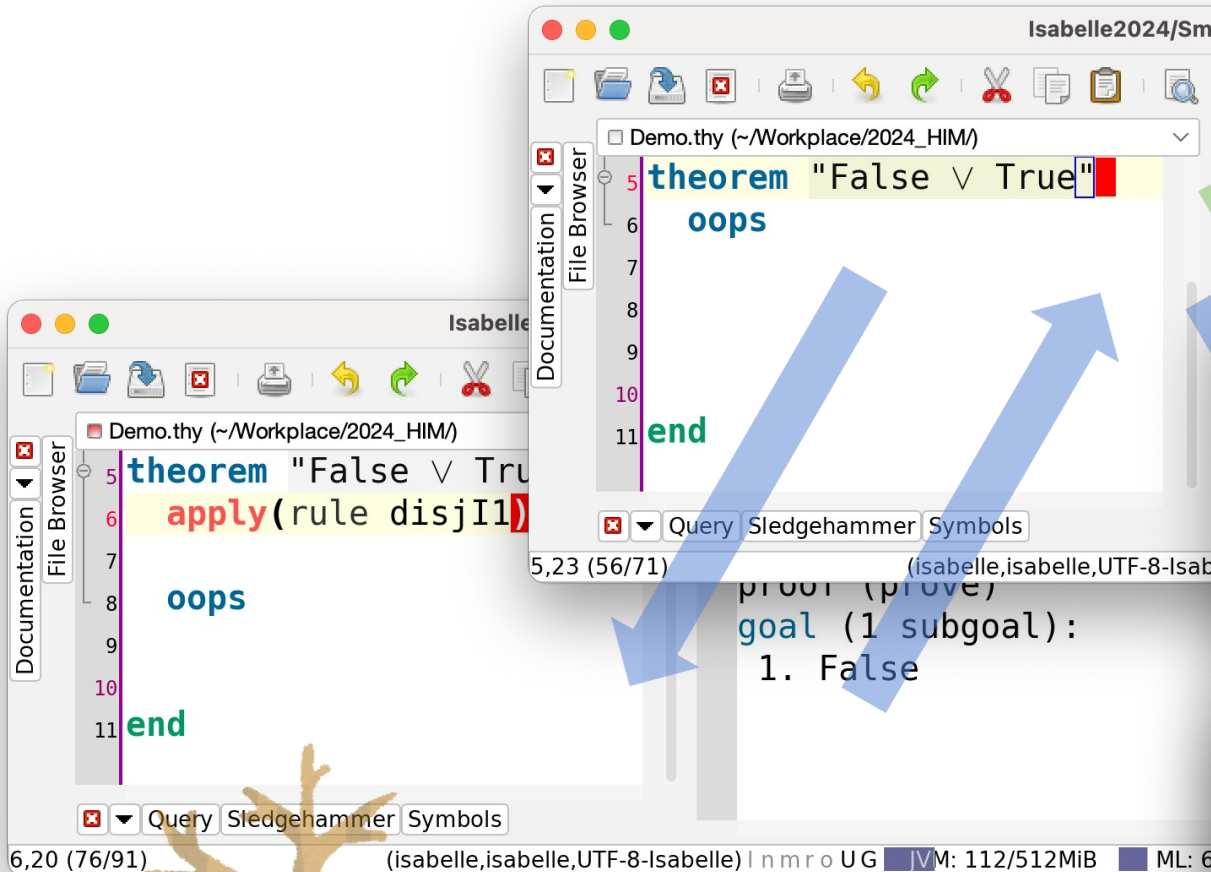
Isabelle2024/Smart_Isabelle - Demo.thy (modified)
5 theorem "False ∨ True"
6   apply(rule disjI2)
7
8   oops
9
10 proof (prove)
11 goal (1 subgoal):
12   1. True
  
```

```

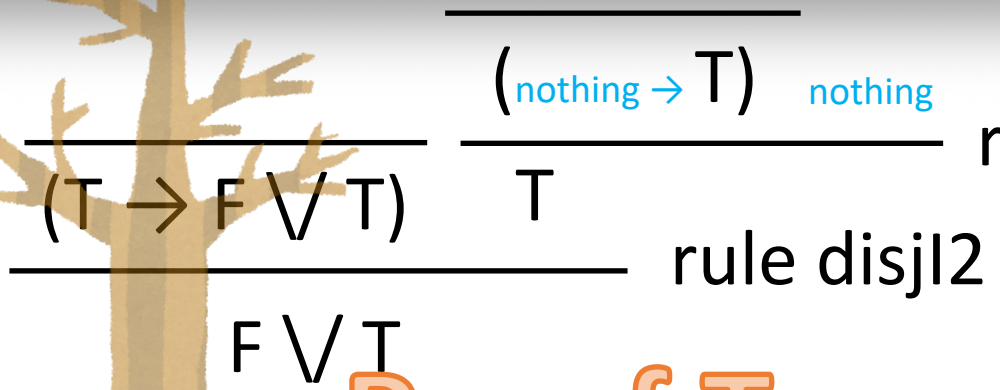
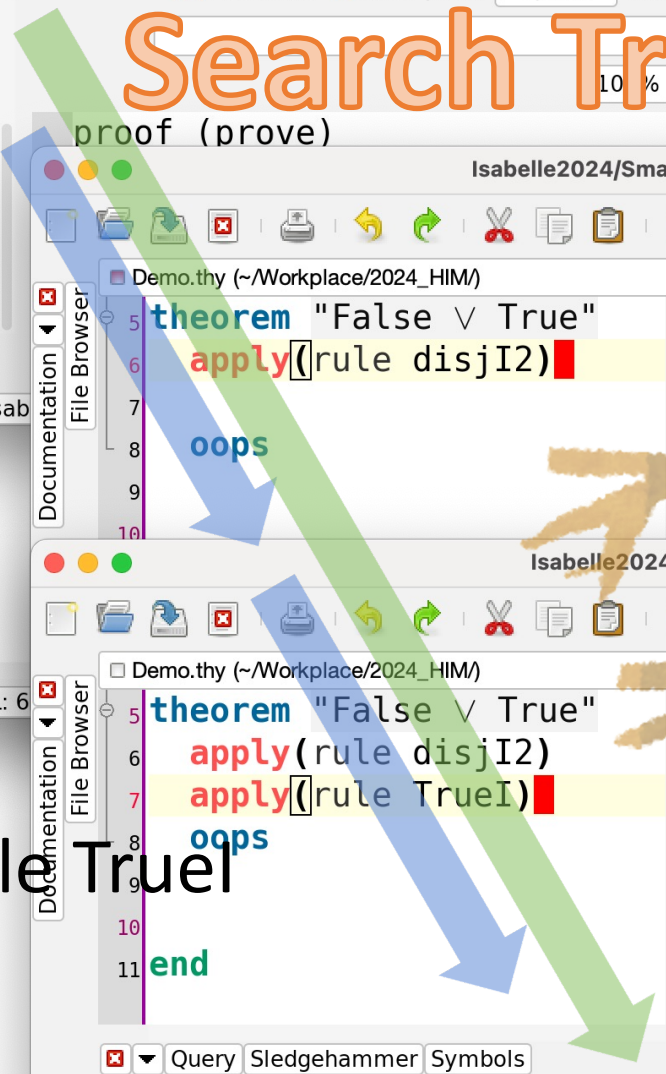
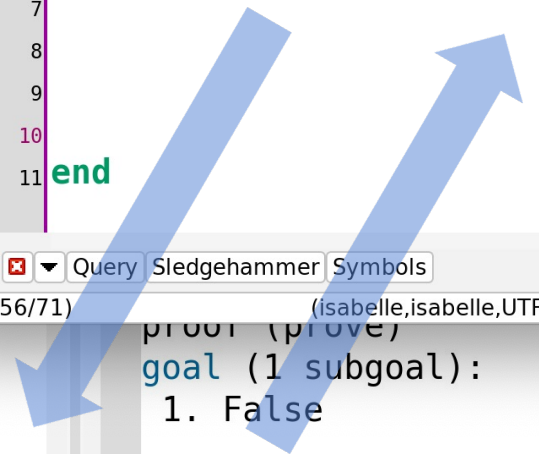
Isabelle2024/Smart_Isabelle - Demo.thy
5 theorem "False ∨ True"
6   apply(rule disjI2)
7   apply(rule TrueI)
8   oops
9
10
11 end
  
```

proof (prove)
goal:
No subgoals!





Search Tree



rule TrueI

Proof Tree

Search Tree



RESEARCH-ARTICLE

PaMpeR: proof method recommendation system for Isabelle/HOL



Authors: Yutaka Nagashima, Yilun He [Authors Info & Affiliations](#)

Publication: ASE 2018: Proceedings of the 33rd ACM/IEEE International Conference on Automated Software Engineering • September 2018 • Pages 362–372 • <https://doi.org/10.1145/3238147.3238210>

4 152

ABSTRACT

Deciding which sub-tool to use in an interactive theorem prover (ITP) is a non-trivial task. We present PaMpeR, a proof method recommendation system for Isabelle/HOL. PaMpeR provides qualitative explanation for its recommendation and generates these recommendations by transferring experienced users' knowledge. PaMpeR correctly recommends a sub-tool, especially when it comes to spe-

References

Faster Smarter Proof by Induction in Isabelle/HOL

Yutaka Nagashima

Proceedings of the Thirtieth International Joint Conference on Artificial Intelligence Main Track. Pages 1981-1988. <https://doi.org/10.24963/ijcai.2021/273>

We present `sem_ind`, a recommendation tool for proof by induction in Isabelle/HOL. Given an inductive problem, `sem_ind` produces candidate arguments for proof by induction, and selects promising ones using heuristics. Our evaluation based on 1,095 inductive problems from 22 source files shows that `sem_ind` improves the accuracy of recommendation from 20.1% to 38.2% for the most promising candidates within 5.0 seconds of timeout compared to its predecessor while decreasing the median value of execution time from 2.79 seconds to 1.06 seconds.

ASE 2018: Proceedings of the 33rd ACM/IEEE...
PaMpeR: proof method recommendation...
Pages 362–372

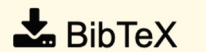
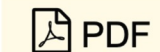
[← Previous](#) [Next →](#)

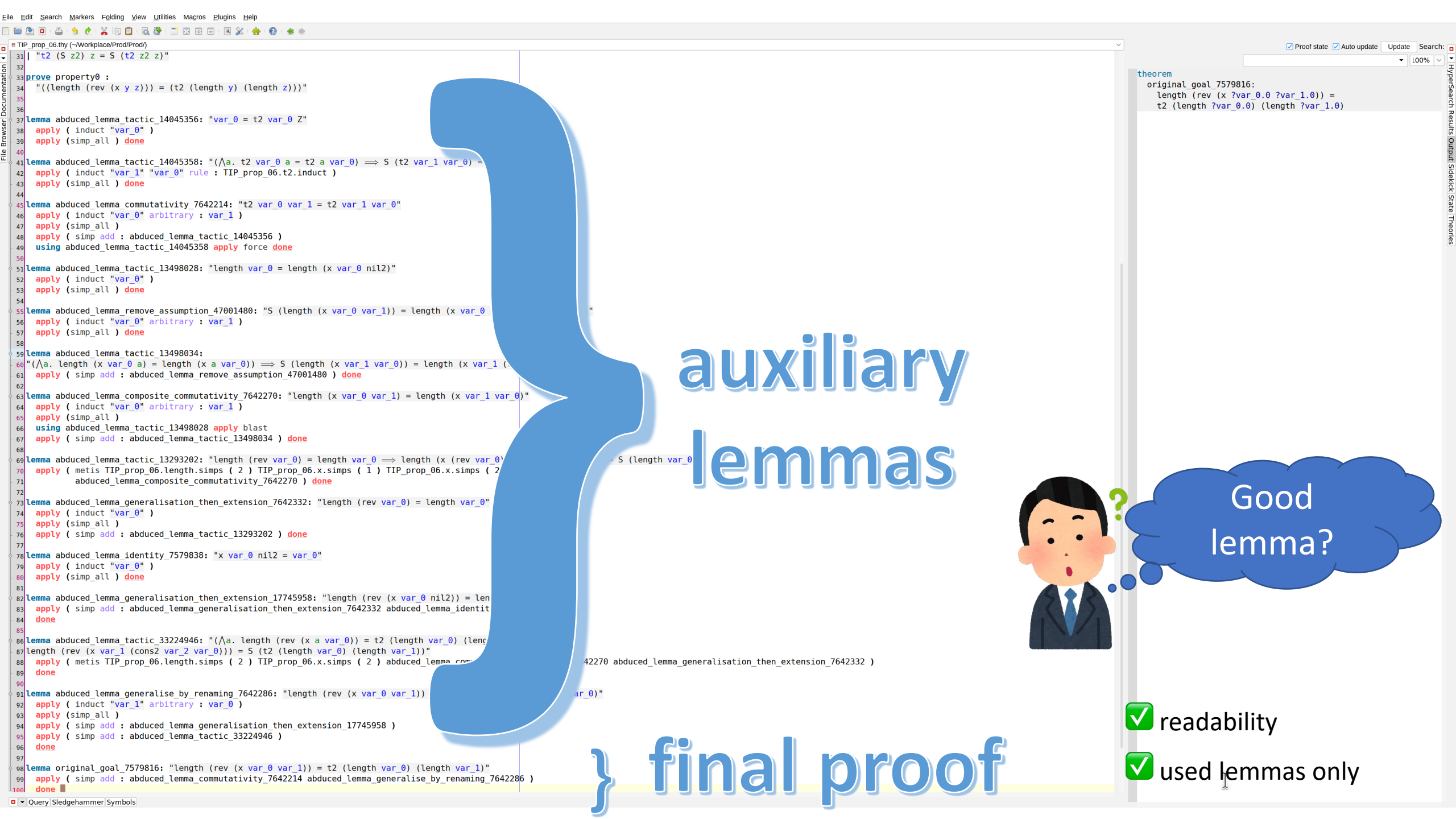
ABSTRACT

References

Index Terms

Comments

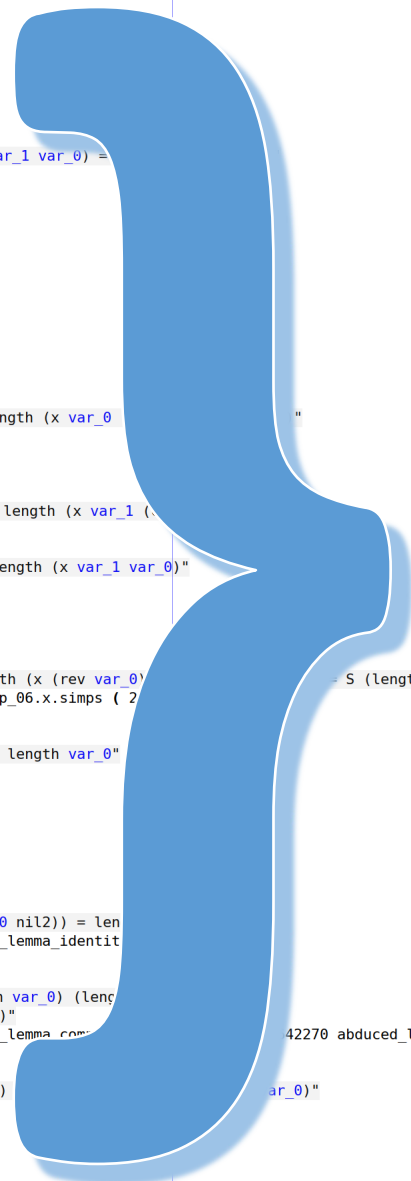




```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36
37 lemma abduced_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply (simp_all ) done
40
41 lemma abduced_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) =
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply (simp_all ) done
44
45 lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply (simp_all )
48   apply (simp add : abduced_lemma_tactic_14045356 )
49   using abduced_lemma_tactic_14045358 apply force done
50
51 lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply (simp_all ) done
54
55 lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply (simp_all ) done
58
59 lemma abduced_lemma_tactic_13498034:
60   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1
61   apply ( simp add : abduced_lemma_remove_assumption_47001480 ) done
62
63 lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply (simp_all )
66   using abduced_lemma_tactic_13498028 apply blast
67   apply ( simp add : abduced_lemma_tactic_13498034 ) done
68
69 lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0)
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71     abduced_lemma_composite_commutativity_7642270 ) done
72
73 lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply (simp_all )
76   apply ( simp add : abduced_lemma_tactic_13293202 ) done
77
78 lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply (simp_all ) done
81
82 lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = len
83   apply ( simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identi
84   done
85
86 lemma abduced_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (lenc
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abduced_lemma_com
89   done
90
91 lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = length (x var_0
92   apply ( induct "var_1" arbitrary : var_0 )
93   apply (simp_all )
94   apply ( simp add : abduced_lemma_generalisation_then_extension_17745958 )
95   apply ( simp add : abduced_lemma_tactic_33224946 )
96   done
97
98 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
99   apply ( simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
100  done

```



auxiliary lemmas

} final proof

theorem
original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)

Good lemma?

✓ readability
✓ used lemmas only



$(P \rightarrow Q) \quad P$

Modus ponens



1. Not obviously false.
2. Useful to prove the goal.
3. Easy to prove.



try to prove

quickcheck

easier

(conjecture \rightarrow goal)

conjecture

Modus ponens

difficult



goal



1. Not obviously false.
2. Useful to prove the goal.
3. Easy to prove.



✓
try to prove

(conjecture → goal)

✓
quickcheck

conjecture

?
easier

Modus ponens

difficult



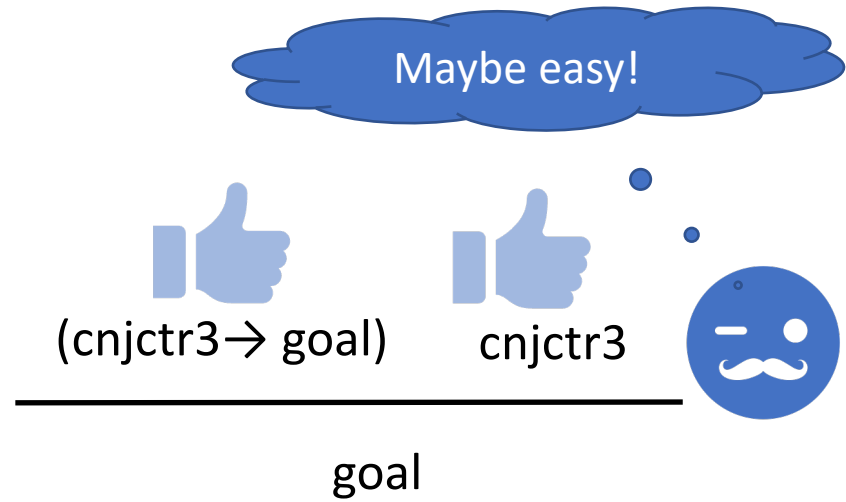
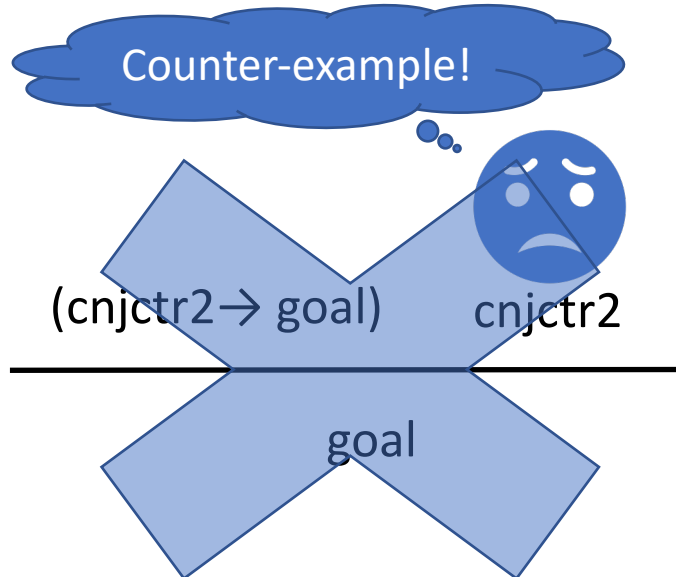
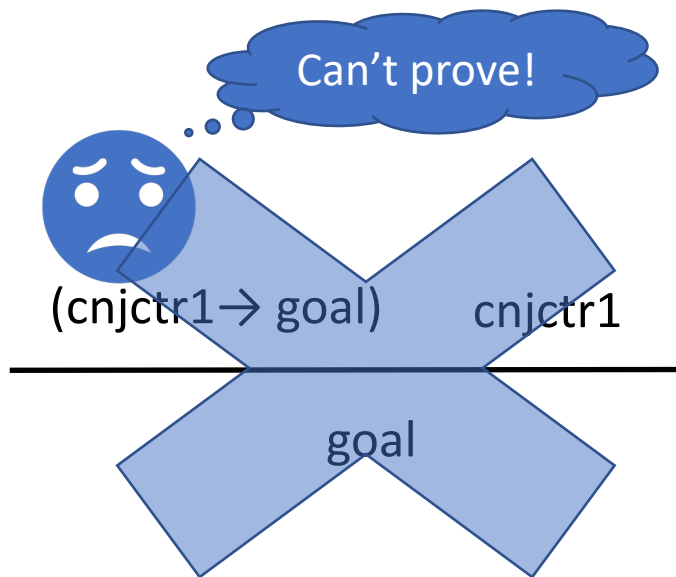
goal

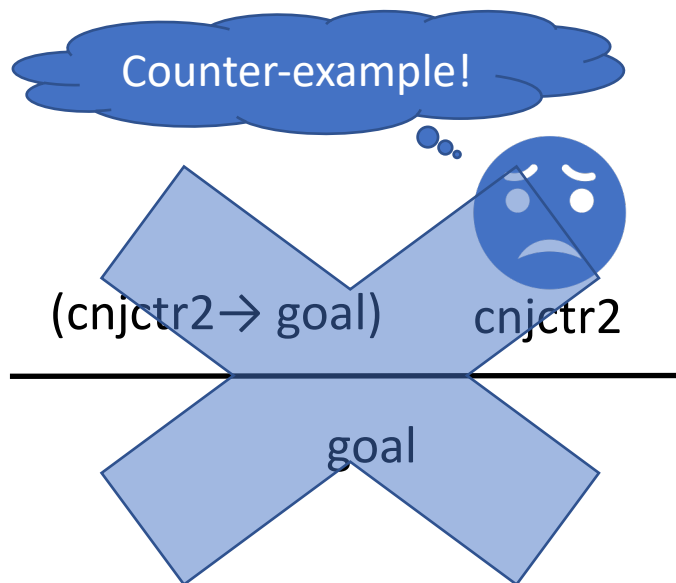
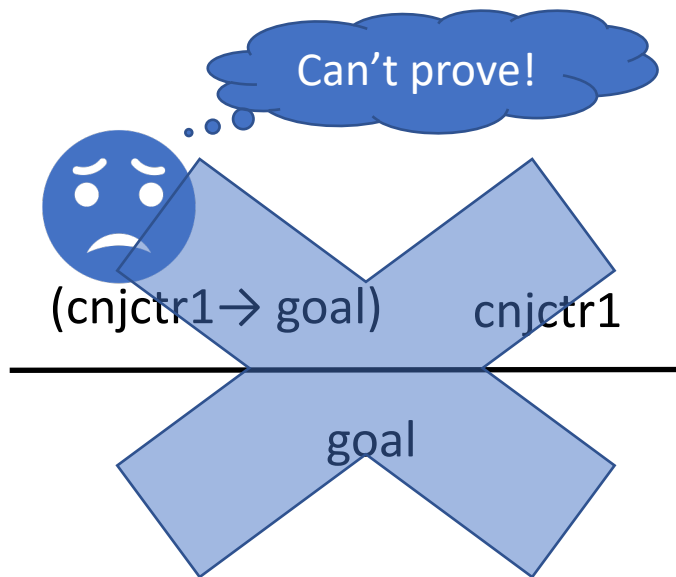
Good lemma?

✓
✓
?

1. Not obviously false.
2. Useful to prove the goal.
3. Easy to prove.







✓
try to prove

(conjecture → goal)

✓
quickcheck

conjecture

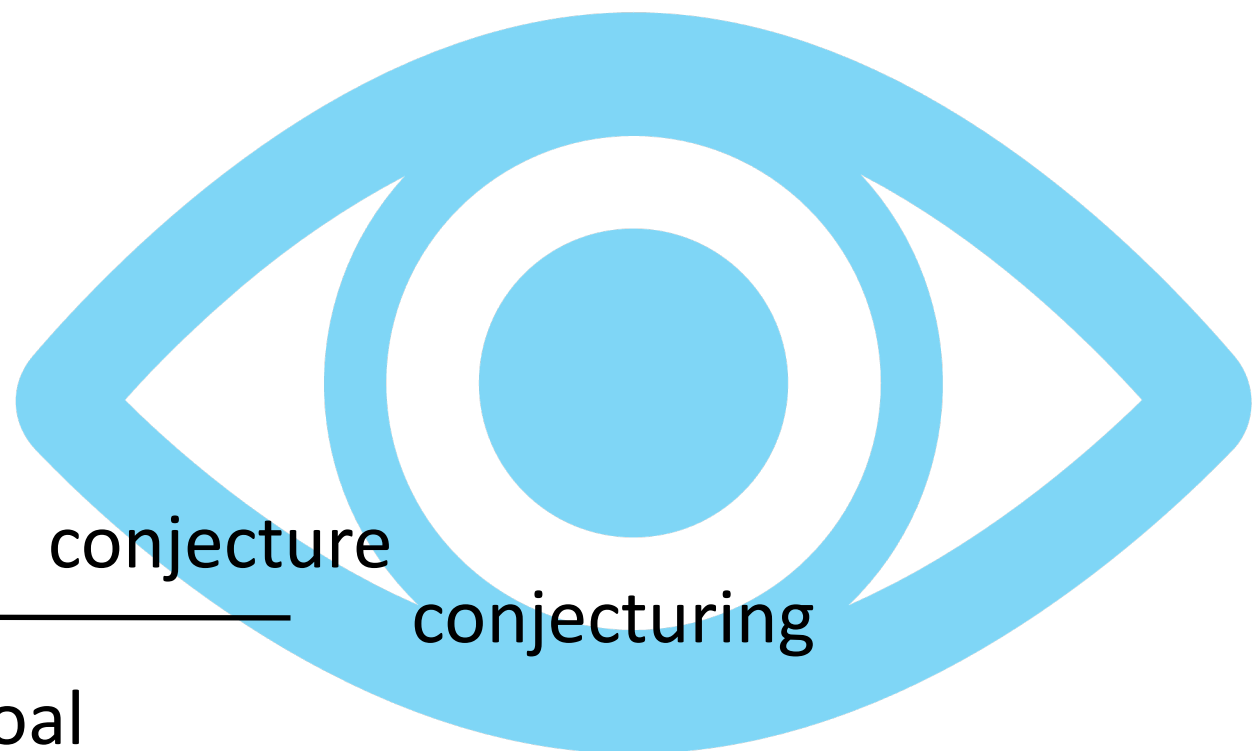
?
easier

conjecturing

goal
difficult

- ✓ 1. Not obviously false.
- ✓ 2. Useful to prove the goal.
- 3. Easy to prove.





(conjecture → goal)

conjecture

conjecturing

goal



I've seen this already.

$$\frac{(T \rightarrow F \vee T) \quad T}{F \vee T} \quad \text{rule disjI2}$$

The screenshot shows the Isabelle2024/Smart_Isabelle interface. The main window displays the following code:

```

5 theorem "False ∨ True"
6   apply(rule disjI2)
7
8   oops
9
10  end

```

The right-hand pane shows the proof state:

```

proof (prove)
goal (1 subgoal):
1. True

```

The status bar at the bottom indicates the file path, encoding, and JVM memory usage.

(conjecture \rightarrow goal) conjecture conjecturing

goal



$\frac{(\text{subgoal} \rightarrow \text{goal}) \quad \text{subgoal}}{\text{goal}}$ tactic application

$\frac{(\text{conjecture} \rightarrow \text{goal}) \quad \text{conjecture}}{\text{goal}}$ conjecturing

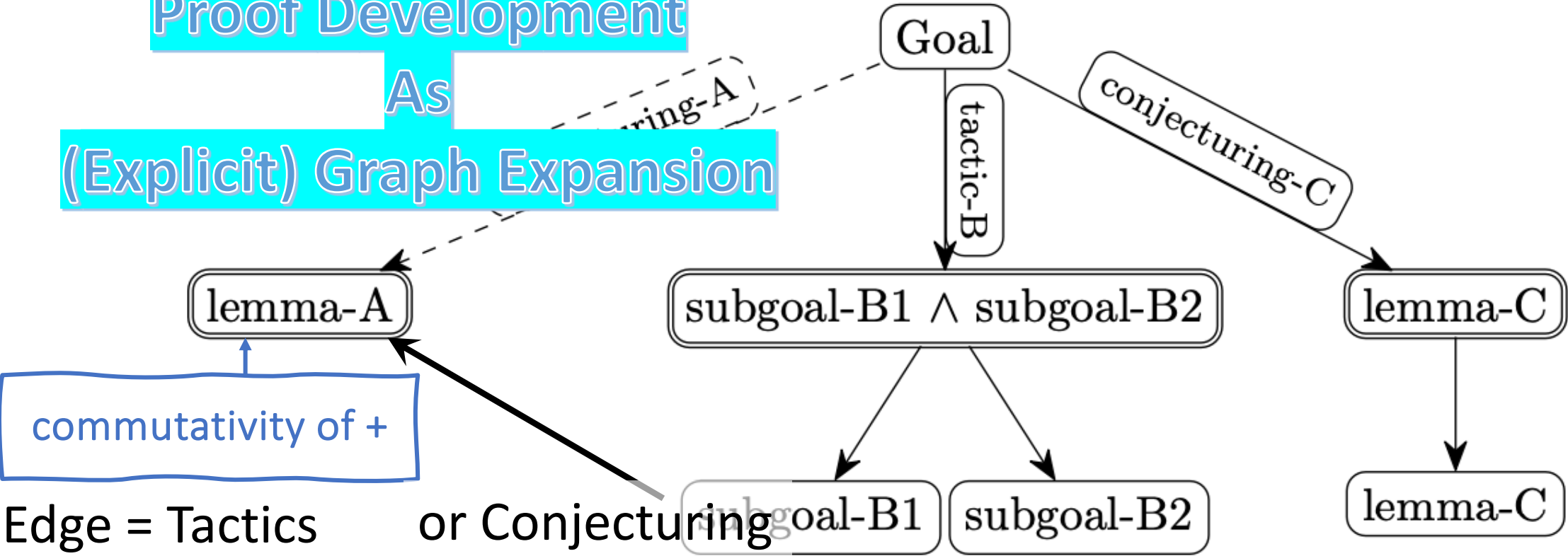


tactic application as conjecturing

Proof Development

As

(Explicit) Graph Expansion



Edge = Tactics or Conjecturing

Node = Subgoals or Auxiliary Lemma

Aim: to find a portion of the graph that represents a proof of the original goal.

LIVE DEMO

(We're almost at the end of this talk.)



TIP_prop_06.thy (~Workplace/Prod/Prod)

```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36
37 lemma abduced_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply ( simp_all ) done
40
41 lemma abduced_lemma_tactic_14045358: "( $\wedge$ a. t2 var_0 a = t2 a var_0)  $\implies$  S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply ( simp_all ) done
44
45 lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply ( simp_all )
48   apply ( simp add : abduced_lemma_tactic_14045356 )
49   using abduced_lemma_tactic_14045358 apply force done
50
51 lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply ( simp_all ) done
54
55 lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply ( simp_all ) done
58
59 lemma abduced_lemma_tactic_13498034:
60   "( $\wedge$ a. length (x var_0 a) = length (x a var_0))  $\implies$  S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply ( simp add : abduced_lemma_remove_assumption_47001480 ) done
62
63 lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply ( simp_all )
66   using abduced_lemma_tactic_13498028 apply blast
67   apply ( simp add : abduced_lemma_tactic_13498034 ) done
68
69 lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0  $\implies$  length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71         abduced_lemma_composite_commutativity_7642270 ) done
72
73 lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply ( simp_all )
76   apply ( simp add : abduced_lemma_tactic_13293202 ) done
77
78 lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply ( simp_all ) done
81
82 lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply ( simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identity_7579838 )
84   done
85
86 lemma abduced_lemma_tactic_33224946: "( $\wedge$ a. length (rev (x a var_0)) = t2 (length var_0) (length a))  $\implies$ 
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abduced_lemma_composite_commutativity_7642270
89         abduced_lemma_generalisation_then_extension_7642332 )
90   done
91 lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
92   apply ( induct "var_1" arbitrary : var_0 )
93   apply ( simp_all )
94   apply ( simp add : abduced_lemma_generalisation_then_extension_17745958 )
95   apply ( simp add : abduced_lemma_tactic_33224946 )
96   done
97
98 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
99   apply ( simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
100  done

```

 Proof state
 Auto update
 Update Search:

100%

theorem

```

original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)

```



```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
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37 lemma abduced_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply ( simp_all ) done
40
41 lemma abduced_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply ( simp_all ) done
44
45 lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply ( simp_all )
48   apply ( simp add : abduced_lemma_tactic_14045356 )
49   using abduced_lemma_tactic_14045358 apply force done
50
51 lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply ( simp_all ) done
54
55 lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply ( simp_all ) done
58
59 lemma abduced_lemma_tactic_13498034:
60   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply ( simp add : abduced_lemma_remove_assumption_47001480 ) done
62
63 lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply ( simp_all )
66   using abduced_lemma_tactic_13498028 apply blast
67   apply ( simp add : abduced_lemma_tactic_13498034 ) done
68
69 lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71     abduced_lemma_composite_commutativity_7642270 ) done
72
73 lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply ( simp_all )
76   apply ( simp add : abduced_lemma_tactic_13293202 ) done
77
78 lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply ( simp_all ) done
81
82 lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply ( simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identity_7579838 )
84   done
85
86 lemma abduced_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (length a)) ==>
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abduced_lemma_composite_commutativity_7642270
89     abduced_lemma_generalisation_then_extension_7642332 )
90   done
91 lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
92   apply ( induct "var_1" arbitrary : var_0 )
93   apply ( simp_all )
94   apply ( simp add : abduced_lemma_generalisation_then_extension_17745958 )
95   apply ( simp add : abduced_lemma_tactic_33224946 )
96   done
97
98 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
99   apply ( simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
100  done

```

(lemma → goal) lemma

Modus ponens

goal

theorem
original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)

100% Search: []

HyperSearch Results Output Sledgehammer Theories

```
TIP_prop_06.thy (~Workplace/Prod/Prod)
31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36
37 lemma abduced_lemma_tactic_14045356 "var_0 = t2 var_0 Z"
38   apply (induct "var_0" )
39   apply (simp_all ) done
40
41 lemma abduced_lemma_tactic_14045358: "( $\wedge a$ . t2 var_0 a = t2 a var_0)  $\implies$  S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply (induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply (simp_all ) done
44
45 lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply (induct "var_0" arbitrary : var_1 )
47   apply (simp_all )
48   apply (simp add : abduced_lemma_tactic_14045356 )
49   using abduced_lemma_tactic_14045358 apply force done
50
51 lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply (induct "var_0" )
53   apply (simp_all ) done
54
55 lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply (induct "var_0" arbitrary : var_1 )
57   apply (simp_all ) done
58
59 lemma abduced_lemma_tactic_13498034:
60   "( $\wedge a$ . length (x var_0 a) = length (x a var_0))  $\implies$  S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply (simp add : abduced_lemma_remove_assumption_47001480 ) done
62
63 lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply (induct "var_0" arbitrary : var_1 )
65   apply (simp_all )
66   using abduced_lemma_tactic_13498028 apply blast
67   apply (simp add : abduced_lemma_tactic_13498034 ) done
68
69 lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0  $\implies$  length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply (metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71     abduced_lemma_composite_commutativity_7642270 ) done
72
73 lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply (induct "var_0" )
75   apply (simp_all )
76   apply (simp add : abduced_lemma_tactic_13293202 ) done
77
78 lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply (induct "var_0" )
80   apply (simp_all ) done
81
82 lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply (simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identity_7579838 )
84   done
85
86 lemma abduced_lemma_tactic_33224946: "( $\wedge a$ . length (rev (x a var_0)) = t2 (length var_0) (length a))  $\implies$ 
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply (metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abduced_lemma_composite_commutativity_7642270 abduced_lemma_generalisation_then_extension_7642332 )
89   done
90
91 lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
92   apply (induct "var_1" arbitrary : var_0 )
93   apply (simp_all )
94   apply (simp add : abduced_lemma_generalisation_then_extension_17745958 )
95   apply (simp add : abduced_lemma_tactic_33224946 )
96   done
97
98 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
99   apply (simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
100  done
```

(lemma \rightarrow goal) lemma
Modus ponens
goal

theorem
original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)

100%

HyperSearch Results Output Sledgehammer Theories

```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36
37 lemma abduced_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply (simp_all ) done
40
41 lemma abduced_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply (simp_all ) done
44
45 lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply (simp_all )
48   apply (simp add : abduced_lemma_tactic_14045356 )
49   using abduced_lemma_tactic_14045358 apply force done
50
51 lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply (simp_all ) done
54
55 lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply (simp_all ) done
58
59 lemma abduced_lemma_tactic_13498034:
60   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply ( simp add : abduced_lemma_remove_assumption_47001480 ) done
62
63 lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply (simp_all )
66   using abduced_lemma_tactic_13498028 apply blast
67   apply ( simp add : abduced_lemma_tactic_13498034 ) done
68
69 lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71         abduced_lemma_composite_commutativity_7642270 ) done
72
73 lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply (simp_all )
76   apply ( simp add : abduced_lemma_tactic_13293202 ) done
77
78 lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply (simp_all ) done
81
82 lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply ( simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identity_7579838 )
84   done
85
86 lemma abduced_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (length a)) ==>
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 )
89         abduced_lemma_composite_commutativity_7642270 abduced_lemma_generalisation_then_extension_7642332 )
90   done
91
92 lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
93   apply ( induct "var_1" arbitrary : var_0 )
94   apply (simp_all )
95   apply ( simp add : abduced_lemma_generalisation_then_extension_17745958 )
96   apply ( simp add : abduced_lemma_tactic_33224946 )
97   done
98
99 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
100   apply ( simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
101   done

```

(lemma → goal) lemma
 Modus ponens
 goal

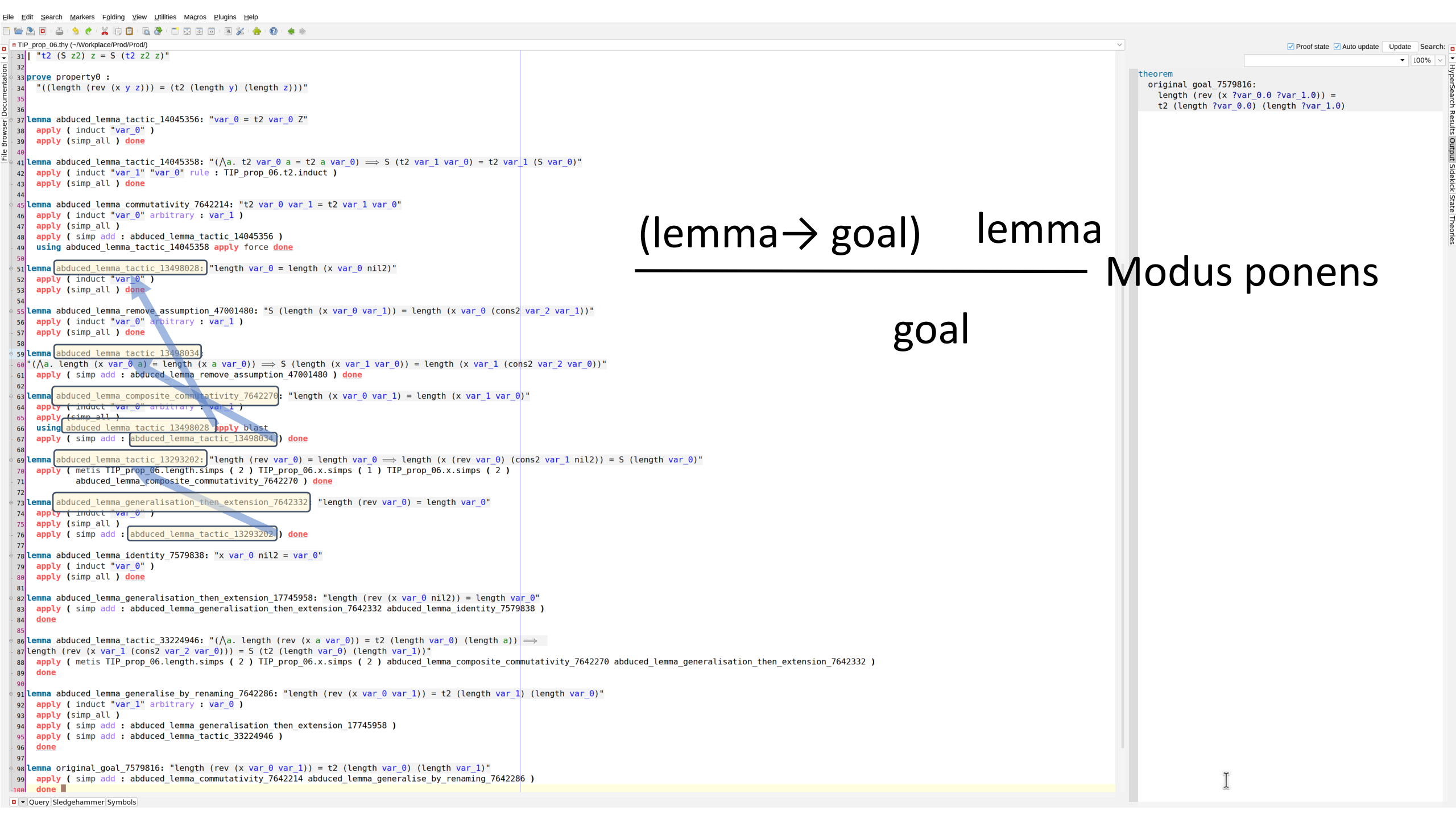
graph instead of tree!



theorem
 original_goal_7579816:
 length (rev (x ?var_0.0 ?var_1.0)) =
 t2 (length ?var_0.0) (length ?var_1.0)

100%

HyperSearch Results Output Sledgehammer Theories



(lemma \rightarrow goal) lemma

goal

Modus ponens

```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36 lemma abduced_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
37   apply ( induct "var_0" )
38   apply ( simp_all ) done
39
40 lemma abduced_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) = t2 var_1 (S var_0)"
41   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
42   apply ( simp_all ) done
43
44 lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
45   apply ( induct "var_0" arbitrary : var_1 )
46   apply ( simp_all )
47   apply ( simp add : abduced_lemma_tactic_14045356 )
48   using abduced_lemma_tactic_14045358 apply force done
49
50 lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
51   apply ( induct "var_0" )
52   apply ( simp_all ) done
53
54 lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
55   apply ( induct "var_0" arbitrary : var_1 )
56   apply ( simp_all ) done
57
58 lemma abduced_lemma_tactic_13498034:
59   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
60   apply ( simp add : abduced_lemma_remove_assumption_47001480 ) done
61
62 lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
63   apply ( induct "var_0" arbitrary : var_1 )
64   apply ( simp_all )
65   using abduced_lemma_tactic_13498028 apply blast
66   apply ( simp add : abduced_lemma_tactic_13498034 ) done
67
68 lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
69   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
70         abduced_lemma_composite_commutativity_7642270 ) done
71
72 lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
73   apply ( induct "var_0" )
74   apply ( simp_all )
75   apply ( simp add : abduced_lemma_tactic_13293202 ) done
76
77 lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
78   apply ( induct "var_0" )
79   apply ( simp_all ) done
80
81 lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
82   apply ( simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identity_7579838 )
83   done
84
85 lemma abduced_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (length a)) ==>
86 length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
87   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abduced_lemma_composite_commutativity_7642270
88         abduced_lemma_generalisation_then_extension_7642332 )
89   done
90
91 lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
92   apply ( induct "var_1" arbitrary : var_0 )
93   apply ( simp_all )
94   apply ( simp add : abduced_lemma_generalisation_then_extension_17745958 )
95   apply ( simp add : abduced_lemma_tactic_33224946 )
96   done
97
98 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
99   apply ( simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
100  done

```

(lemma → goal) lemma
 Modus ponens
 goal

← already checked it was proved

← because it was used here.

graph instead of tree!

theorem
 original_goal_7579816:
 length (rev (x ?var_0.0 ?var_1.0)) =
 t2 (length ?var_0.0) (length ?var_1.0)





Q & A

3 take-home lessons:

Domain-Specific
Language

Smart Induction

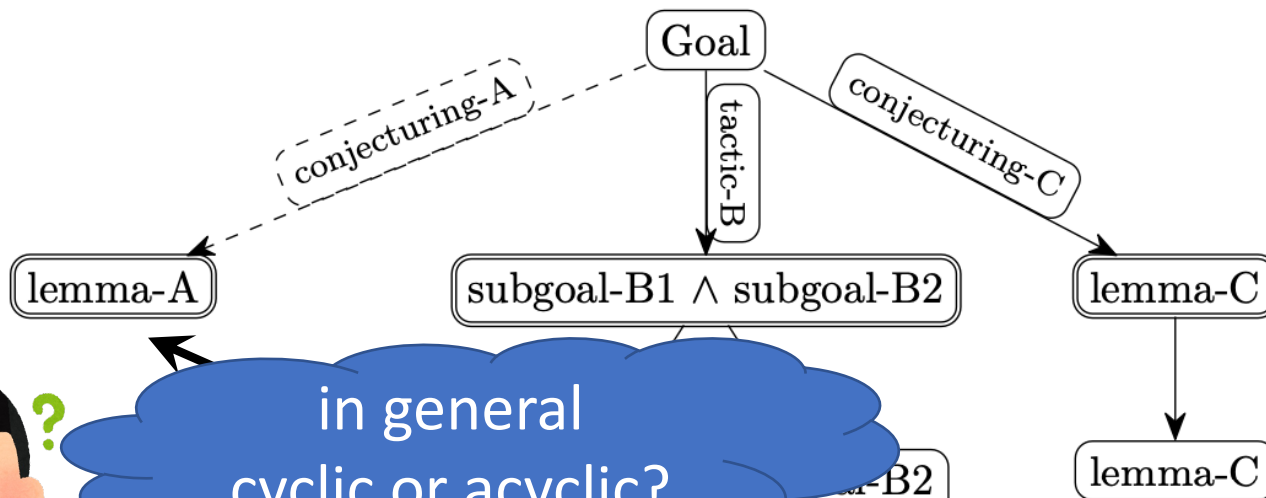
Evaluation Results

Parallelism

Many-Step Abduction

Simultaneous Abduction

Definitinal Quantifiers





```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36
37 Lemma abduced_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply (simp_all ) done
40
41 Lemma abduced_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply (simp_all ) done
44
45 Lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply (simp_all )
48   apply ( simp add : abduced_lemma_tactic_14045356 )
49   using abduced_lemma_tactic_14045358 apply force done
50
51 Lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply (simp_all ) done
54
55 Lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply (simp_all ) done
58
59 Lemma abduced_lemma_tactic_13498034:
60   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply ( simp add : abduced_lemma_remove_assumption_47001480 ) done
62
63 Lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply (simp_all )
66   using abduced_lemma_tactic_13498028 apply blast
67   apply ( simp add : abduced_lemma_tactic_13498034 ) done
68
69 Lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71     abduced_lemma_composite_commutativity_7642270 ) done
72
73 Lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply (simp_all )
76   apply ( simp add : abduced_lemma_tactic_13293202 ) done
77
78 Lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply (simp_all ) done
81
82 Lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply ( simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identity_7579838 )
84   done
85
86 Lemma abduced_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (length a)) ==>
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abduced_lemma_composite_commutativity_7642270
89     abduced_lemma_generalisation_then_extension_7642332 )
90   done
91
92 Lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
93   apply ( induct "var_1" arbitrary : var_0 )
94   apply (simp_all )
95   apply ( simp add : abduced_lemma_generalisation_then_extension_17745958 )
96   apply ( simp add : abduced_lemma_tactic_33224946 )
97   done
98
99 Lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
100   apply ( simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
101   done

```

(lemma → goal) lemma

modus ponens

goal

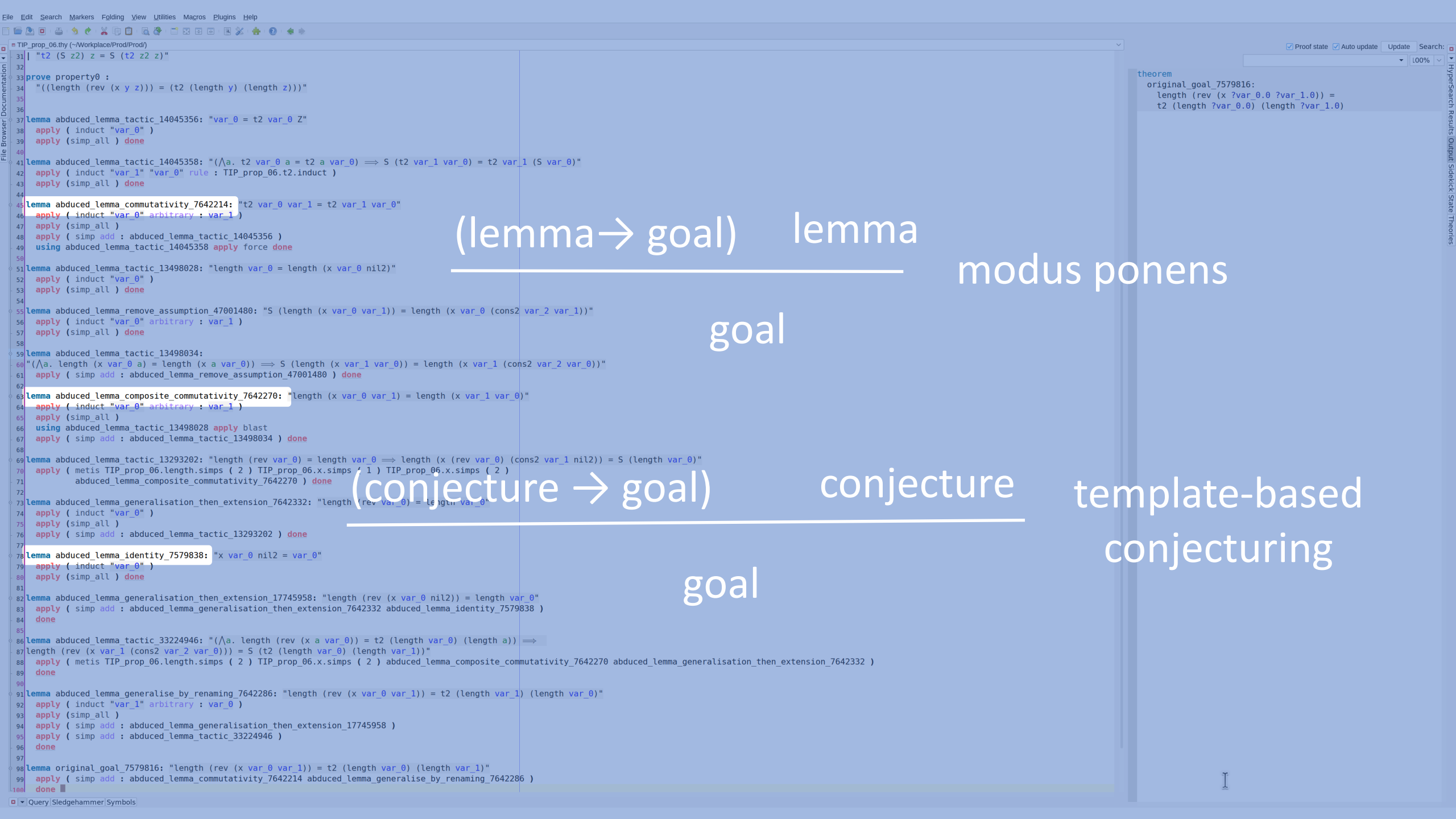
(sub-goal → goal) sub-goal

tactic

goal

application

theorem
original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)



(lemma → goal) lemma

modus ponens

goal

(conjecture → goal) conjecture

conjecture

template-based

conjecturing

goal

theorem
original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)

```
31 | "t2 (S z2) z = S (t2 z2 z)"
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33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
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37 lemma abducted_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply (simp_all ) done
40
41 lemma abducted_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply (simp_all ) done
44
45 lemma abducted_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply (simp_all )
48   apply ( simp add : abducted_lemma_tactic_14045356 )
49   using abducted_lemma_tactic_14045358 apply force done
50
51 lemma abducted_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply (simp_all ) done
54
55 lemma abducted_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply (simp_all ) done
58
59 lemma abducted_lemma_tactic_13498034:
60   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply ( simp add : abducted_lemma_remove_assumption_47001480 ) done
62
63 lemma abducted_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply (simp_all )
66   using abducted_lemma_tactic_13498028 apply blast
67   apply ( simp add : abducted_lemma_tactic_13498034 ) done
68
69 lemma abducted_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71     abducted_lemma_composite_commutativity_7642270 ) done
72
73 lemma abducted_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply (simp_all )
76   apply ( simp add : abducted_lemma_tactic_13293202 ) done
77
78 lemma abducted_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply (simp_all ) done
81
82 lemma abducted_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply ( simp add : abducted_lemma_generalisation_then_extension_7642332 abducted_lemma_identity_7579838 )
84   done
85
86 lemma abducted_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (length a)) ==>
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abducted_lemma_composite_commutativity_7642270
89     abducted_lemma_generalisation_then_extension_7642332 )
90   done
91
92 lemma abducted_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
93   apply ( induct "var_1" arbitrary : var_0 )
94   apply (simp_all )
95   apply ( simp add : abducted_lemma_generalisation_then_extension_17745958 )
96   apply ( simp add : abducted_lemma_tactic_33224946 )
97   done
98
99 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
100   apply ( simp add : abducted_lemma_commutativity_7642214 abducted_lemma_generalise_by_renaming_7642286 )
101   done
```

```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36
37 lemma abducted_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply (simp_all ) done
40
41 lemma abducted_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply (simp_all ) done
44
45 lemma abducted_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply (simp_all )
48   apply ( simp add : abducted_lemma_tactic_14045356 )
49   using abducted_lemma_tactic_14045358 apply force done
50
51 lemma abducted_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply (simp_all ) done
54
55 lemma abducted_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply (simp_all ) done
58
59 lemma abducted_lemma_tactic_13498034:
60   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply ( simp add : abducted_lemma_remove_assumption_47001480 ) done
62
63 lemma abducted_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply (simp_all )
66   using abducted_lemma_tactic_13498028 apply blast
67   apply ( simp add : abducted_lemma_tactic_13498034 ) done
68
69 lemma abducted_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71     abducted_lemma_composite_commutativity_7642270 ) done
72
73 lemma abducted_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply (simp_all )
76   apply ( simp add : abducted_lemma_tactic_13293202 ) done
77
78 lemma abducted_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply (simp_all ) done
81
82 lemma abducted_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply ( simp add : abducted_lemma_generalisation_then_extension_7642332 abducted_lemma_identity_7579838 )
84   done
85
86 lemma abducted_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (length a)) ==>
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abducted_lemma_composite_commutativity_7642270
89     abducted_lemma_generalisation_then_extension_7642332 )
90   done
91
92 lemma abducted_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
93   apply ( induct "var_1" arbitrary : var_0 )
94   apply (simp_all )
95   apply ( simp add : abducted_lemma_generalisation_then_extension_17745958 )
96   apply ( simp add : abducted_lemma_tactic_33224946 )
97   done
98
99 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
100   apply ( simp add : abducted_lemma_commutativity_7642214 abducted_lemma_generalise_by_renaming_7642286 )
101   done

```

(lemma → goal) lemma

modus ponens

goal

(conjecture → goal)

conjecture

mutation-based conjecturing

goal

Proof state Auto update Update Search

100%

theorem
original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)

HyperSearch Results Output Selected State Theories

```

31 | "t2 (S z2) z = S (t2 z2 z)"
32
33 prove property0 :
34   "((length (rev (x y z))) = (t2 (length y) (length z)))"
35
36
37 lemma abduced_lemma_tactic_14045356: "var_0 = t2 var_0 Z"
38   apply ( induct "var_0" )
39   apply (simp_all ) done
40
41 lemma abduced_lemma_tactic_14045358: "(/a. t2 var_0 a = t2 a var_0) ==> S (t2 var_1 var_0) = t2 var_1 (S var_0)"
42   apply ( induct "var_1" "var_0" rule : TIP_prop_06.t2.induct )
43   apply (simp_all ) done
44
45 lemma abduced_lemma_commutativity_7642214: "t2 var_0 var_1 = t2 var_1 var_0"
46   apply ( induct "var_0" arbitrary : var_1 )
47   apply (simp_all )
48   apply ( simp add : abduced_lemma_tactic_14045356 )
49   using abduced_lemma_tactic_14045358 apply force done
50
51 lemma abduced_lemma_tactic_13498028: "length var_0 = length (x var_0 nil2)"
52   apply ( induct "var_0" )
53   apply (simp_all ) done
54
55 lemma abduced_lemma_remove_assumption_47001480: "S (length (x var_0 var_1)) = length (x var_0 (cons2 var_2 var_1))"
56   apply ( induct "var_0" arbitrary : var_1 )
57   apply (simp_all ) done
58
59 lemma abduced_lemma_tactic_13498034:
60   "(/a. length (x var_0 a) = length (x a var_0)) ==> S (length (x var_1 var_0)) = length (x var_1 (cons2 var_2 var_0))"
61   apply ( simp add : abduced_lemma_remove_assumption_47001480 ) done
62
63 lemma abduced_lemma_composite_commutativity_7642270: "length (x var_0 var_1) = length (x var_1 var_0)"
64   apply ( induct "var_0" arbitrary : var_1 )
65   apply (simp_all )
66   using abduced_lemma_tactic_13498028 apply blast
67   apply ( simp add : abduced_lemma_tactic_13498034 ) done
68
69 lemma abduced_lemma_tactic_13293202: "length (rev var_0) = length var_0 ==> length (x (rev var_0) (cons2 var_1 nil2)) = S (length var_0)"
70   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 1 ) TIP_prop_06.x.simps ( 2 )
71     abduced_lemma_composite_commutativity_7642270 ) done
72
73 lemma abduced_lemma_generalisation_then_extension_7642332: "length (rev var_0) = length var_0"
74   apply ( induct "var_0" )
75   apply (simp_all )
76   apply ( simp add : abduced_lemma_tactic_13293202 ) done
77
78 lemma abduced_lemma_identity_7579838: "x var_0 nil2 = var_0"
79   apply ( induct "var_0" )
80   apply (simp_all ) done
81
82 lemma abduced_lemma_generalisation_then_extension_17745958: "length (rev (x var_0 nil2)) = length var_0"
83   apply ( simp add : abduced_lemma_generalisation_then_extension_7642332 abduced_lemma_identity_7579838 )
84   done
85
86 lemma abduced_lemma_tactic_33224946: "(/a. length (rev (x a var_0)) = t2 (length var_0) (length a)) ==>
87   length (rev (x var_1 (cons2 var_2 var_0))) = S (t2 (length var_0) (length var_1))"
88   apply ( metis TIP_prop_06.length.simps ( 2 ) TIP_prop_06.x.simps ( 2 ) abduced_lemma_composite_commutativity_7642270 abduced_lemma_generalisation_then_extension_7642332 )
89   done
90
91 lemma abduced_lemma_generalise_by_renaming_7642286: "length (rev (x var_0 var_1)) = t2 (length var_1) (length var_0)"
92   apply ( induct "var_1" arbitrary : var_0 )
93   apply (simp_all )
94   apply ( simp add : abduced_lemma_generalisation_then_extension_17745958 )
95   apply ( simp add : abduced_lemma_tactic_33224946 )
96   done
97
98 lemma original_goal_7579816: "length (rev (x var_0 var_1)) = t2 (length var_0) (length var_1)"
99   apply ( simp add : abduced_lemma_commutativity_7642214 abduced_lemma_generalise_by_renaming_7642286 )
100  done

```

simultaneous
conjecturing

(lemma1 → Imma2 → goal) lemma1 lemma2

goal

Proof state Auto update Update Search

100%

theorem
original_goal_7579816:
length (rev (x ?var_0.0 ?var_1.0)) =
t2 (length ?var_0.0) (length ?var_1.0)

HyperSearch Results Output Selectick State Theories